Chapter 3 Describing Syntax and Semantics

3.1 Introduction

- Providing a concise yet understandable description of a programming language is difficult but essential to the language's success.
 - ALGOL 60 and ALGOL 68 were first.
- For programming language implementors
- Language reference manual

3.1 Introduction (Cont'd)

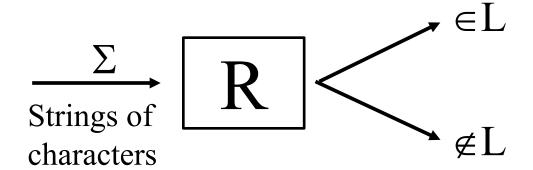
- Definition of Syntax and Semantics
 - Syntax:
 - Form, context-free
 - Semantics:
 - Meaning, context-sensitive

3.2 The General Problem of Describing Syntax

- Alphabet, Strings, Sentences, Language
- Lexemes and Tokens

3.2.1 Language Recognizers

• R: Recognition device



3.2.1 Language Recognizers

• G: Language generator

$$R \longrightarrow A \text{ sentence of } L$$

3.3 Formal Methods of Describing Syntax

- Backus-Naur Form and Context-free Grammars
 - Appeared in late 1950s
 - Context-free Grammers
 - Chomsky, a noted linguist, advised it.
 - Context-free and regular grammars turned out to be useful for describing the syntax of programming languages
 - » Context-free grammar: Syntax
 - » Regular grammar: Token

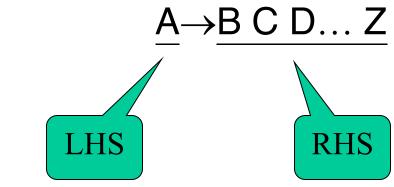
3.3 Formal Methods of Describing Syntax

- Backus-Naur Form
 - Shortly after Chomsky's work
 - John Backus and Peter Naur
 - Describing the syntax of ALGOL 58
 - BNF

- Fundamentals
 - A metalanguage is a language that is used to describe another language.
 - E.g., BNF

Context-free grammar (CFG)

CFG consists of a set of production rules,



LHS must be a single nonterminal

RHS consists 0 or more terminals or nonterminals

Context-free grammar (CFG)

- Two kinds of symbols
 - Nonterminals
 - Delimited by < and >
 - Represent syntactic structures
 - Terminals
 - Represent tokens
- E.g.

```
opram> \rightarrow begin <statement list> end
```

- Start or goal symbol
- λ : empty or null string

Context-free grammar (Cont'd)

• E.g.

```
<statement list> \rightarrow <statement><statement tail> <statement tail> \rightarrow \lambda <statement tail> \rightarrow <statement tail>
```

Context-free grammar (Cont'd)

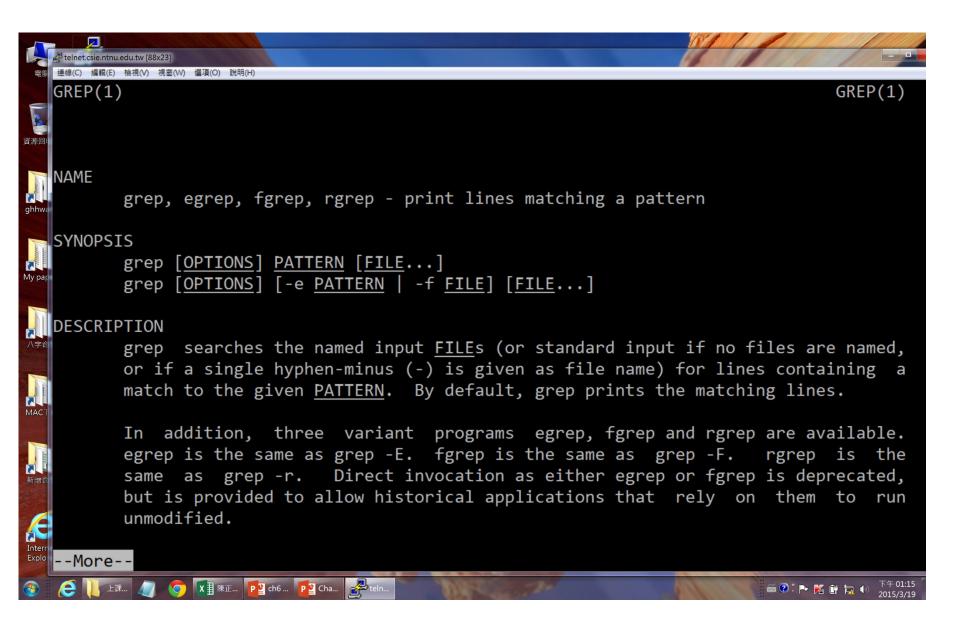
Extended BNF: some abbreviations

```
1. optional: [] 0 or 1
       \langle stmt \rangle \rightarrow if \langle exp \rangle then \langle stmt \rangle
       \langle \text{stmt} \rangle \rightarrow \text{if } \langle \text{exp} \rangle \text{ then } \langle \text{stmt} \rangle = \text{else } \langle \text{stmt} \rangle
       can be written as
       \langle stmt \rangle \rightarrow if \langle exp \rangle then \langle stmt \rangle [else \langle stmt \rangle]
2. repetition: {} 0 or more
       <stmt list> → <stmt> <tail>
       \langle \text{tail} \rangle \rightarrow \lambda
       <tail> → <stmt> <tail>
       can be written as
       \langle \text{stmt list} \rangle \rightarrow \langle \text{stmt} \rangle  { \langle \text{stmt} \rangle  }
```

Context-free grammar (Cont'd)

Extended BNF: some abbreviations

- - Either can be transformed to the other.
 - Extended BNF is more compact and readable



The Syntax of Micro (Cont'd)

```
→ begin <statement list> end
     cprogram>
                      → <statement> {<statement>}
2.
     <statement list>
                      \rightarrow ID := <expression>;
3.
   <statement>
                      \rightarrow read ( <id list> );
4.
   <statement>
                      → write ( <expr list> );
5. <statement>
                      \rightarrow ID \{, ID\}
6. <id list>
7. <expr list>
                      → <expression> {, <expression>}
                      → <pri>primary> {<add op> <primary>}
8.
     <expression>
                      → ( <expression> )
     cprimary>
9.
     <primary>
10.
                      \rightarrow ID
11.
     rimary>
                      → INTLITERAL
     <add op>
                      → PLUSOP
12.
                      → MINUSOP
     <add op>
13.
                      14.
     <system goal>
```

Figure 2.4 Extended CFG Defining Micro

• The derivation of

begin ID:= ID + (INTLITERAL – ID); end

```
cprogram>
⇒ begin <statement list> end
                                                               (Apply rule 1)
⇒ begin <statement> {<statement>} end
                                                               (Apply rule 2)
⇒ begin <statement> end
                                                               (Choose 0 repetitions)
⇒ begin ID := <expression> ; end
                                                               (Apply rule 3)
⇒ begin ID := <primary> {<add op> <primary>} ; end
                                                               (Apply rule 8)
⇒ begin ID := <pri>primary> <add op> <primary> ; end</pr>
                                                               (Choose 1 repetition)
⇒ begin ID := <primary> + <primary> ; end
                                                               (Apply rule 12)
                                                               (Apply rule 10)
⇒ begin ID := ID + <pri>primary> ; end
                                                               (Apply rule 9)
⇒ begin ID := ID + ( <expression> ) ; end
                                                               (Apply rule 8)
⇒ begin ID := ID + ( <primary> {<add op> <primary>} ) ; end
⇒ begin ID := ID + ( <primary> <add op> <primary> ) ; end
                                                               (Choose 1 repetition)
⇒ begin ID := ID + ( <primary> - <primary> ); end
                                                               (Apply rule 13)
⇒ begin ID := ID + (INTLITERAL - <pri>primary>); end
                                                               (Apply rule 11)
                                                               (Apply rule 10)
⇒ begin ID := ID + ( INTLITERAL – ID ) ; end
```

- Describing Lists
 - Variable-length lists in mathematics are often written using an ellipsis (...)
 - For BNF, the alternative is recursion

- Grammars and Derivations
 - start symbol
 - derivation
 - sentential form & leftmost derivations
 - See next slice

• A grammar

• A derivation

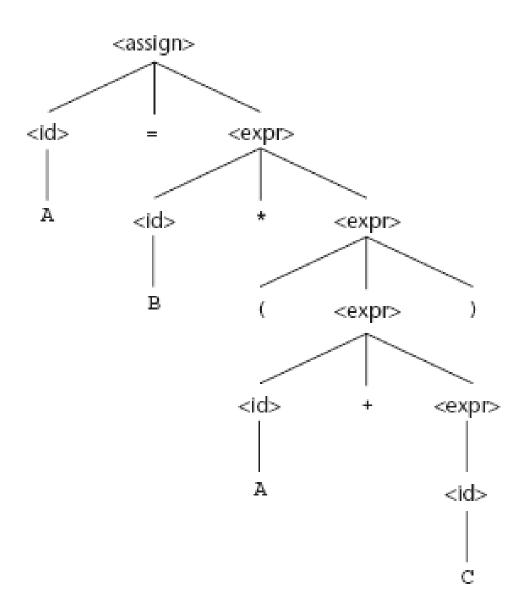
Parse trees

- One of the most attractive features of grammars is that they naturally describe the hierarchical syntactic structure of the sentences of the languages they define.
 - Internal node: nonterminal symbol
 - Leaf node: terminal symbol

Figure 3.1

A parse tree for the simple statement

$$A = B * (A + C)$$



- Ambiguity
 - A grammar that generates a sentential form for which there are two or more distinct parse tree is said to be ambiguous
 - See next slice
 - Why may ambiguity cause problem?
 - Code generation for compilers

Figure 3.2

Two distinct parse trees for the same sentence, A = B + C * A

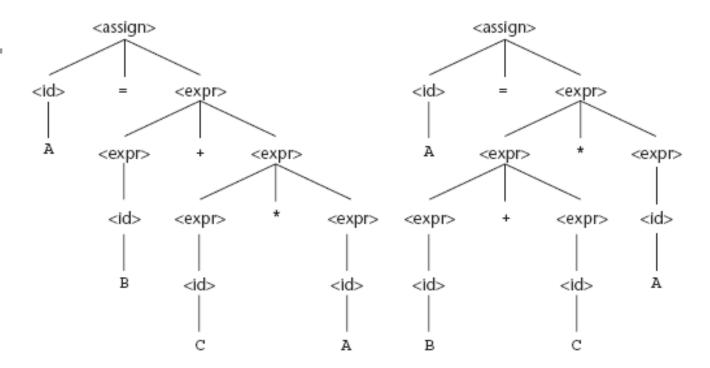
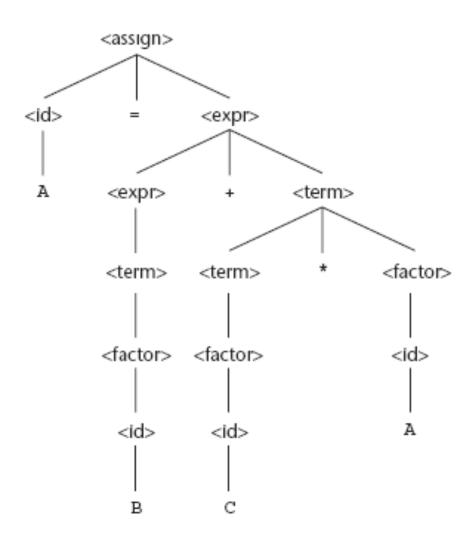


Fig1.2

- Operator precedence
 - The order of evaluation of operators
 - Can the BNF demonstrate the operator precedence?
 - See EXAMPLE 3.4 and the derivation of A=B+C *A

Figure 3.3

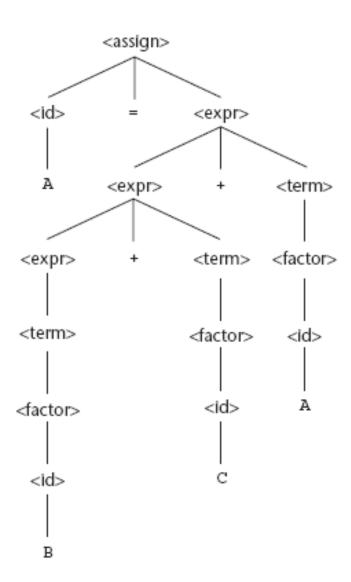
The unique parse tree for A = B + C * A using an unambiguous grammar



- Associativity of operators
 - When an expression includes two operators that have the same precedence, a semantic rule is required to specify which should have precedence
 - The left recursion specifies left associativity

Figure 3.4

A parse tree for A = B + C + A illustrating the associativity of addition

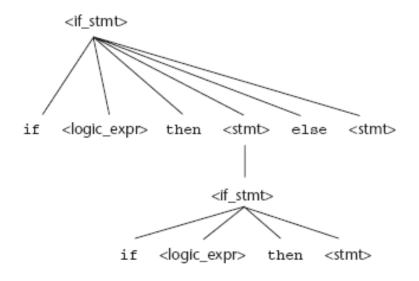


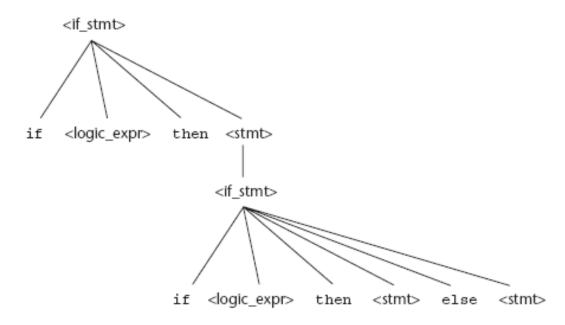
An unambiguous grammar for ifthen-else

An intuitive BNF for if-then-else

Figure 3.5

Two distinct parse trees for the same sentential form





An unambiguous grammar for ifthen-else

• The unambiguous grammar